

# Lecture 4 (Part-1)

# Practical Issues: Beam Injection and Extraction

Chandra Bhat



### Beam Injection and Extraction

<u>Goal:</u> Achieve transfer of beam from one machine to another with a.No beam loss

b.No emittance growth

There are several beam injection and extraction schemes in use . Each scheme is specific to the requirement.

1.Fast injection and extraction

- 2.Multi-turn injection and Phase-space painting
- 3. Charge-exchange injection
- 4. Resonant extraction
- 5.Combined stacking and cooling
- 6.Longitudinal Phase-space coating

Fast (single-turn) Injection and Extraction:

The most straight forward way of beam injection and extraction is by using ,

a.Fast kicker

b. Septum

This is an electrostatic or magnetic device that provides an angular deflection to the beam. The rise and fall time of the kicker is generally in the range of a few nsec to 100 nsec.

This is a device with an aperture divided into 1.Field-free region

2.Uniform field region



### Kickers and Septum Magnets





#### MI NiMI Lam.



#### Fermilab Debuncher Septum



Main Injector



### Injection and Extraction (cont.)

<u>Injection</u>: The beam is injected onto the central orbit of a synchrotron via a septum unit and a fast kicker with appropriate matching in both transverse and longitudinal planes.

<u>Extraction</u>: Kicker is used to deflect the beam from the central orbit onto an extraction orbit and onto the field region aperture of the septum.

For both injection and extraction a FODO cell is used with a phase advance of  $\pi/2$ .



In the case of injection, the first requirement is that the lattice functions have to be matched at the entry point of the ring.

→  $\beta_x$ ,  $\alpha_x$ ,  $\beta_y$ ,  $\alpha_y$ ,  $D_x$ ,  $D_x'$ ,  $D_y$  and  $D_y'$ , at the exit from the septum unit must be identical to the ring lattice parameters at that point.

The reverse is for beam extraction.



### Injection and Extraction (cont.)

Calculation of the Kick Angle:

The kick on the closed orbit to bump the beam into an extraction channel is similar to introducing a transient dipole error at the transfer point in a perfect lattice.

$$\begin{bmatrix} x \\ x' \end{bmatrix} = \begin{bmatrix} \sqrt{\frac{\beta}{\beta_0}} [\cos(\Delta \psi) + \alpha \sin(\Delta \psi)] & \sqrt{\beta\beta_0} \sin(\Delta \psi) \\ \sqrt{\frac{1}{\beta\beta_0}} [(\alpha_0 - \alpha) \cos(\Delta \psi) - (1 + \alpha\alpha_0) \sin(\Delta \psi)] & \sqrt{\frac{\beta_0}{\beta}} [\cos(\Delta \psi) - \alpha \sin(\Delta \psi)] \end{bmatrix} \begin{bmatrix} 0 \\ \theta \end{bmatrix}_k$$
  
$$\therefore \quad \theta_k = x_{close}(s) / \sqrt{\beta_x(s_k)\beta_x(s)} \sin(\Delta \psi) \quad \text{with } \beta = \beta_x(s) \& \beta_0 = \beta_x(s_k) \quad ---- 1$$

where  $\theta_k = \frac{\int B_k ds}{B\rho}$ 

is the kicker strength.  $B_k$  is kicker dipole field.  $\Delta \psi$  is the phase advance between kicker location to that of the septum.

From Eq. 1 it may be seen that a high value of  $\beta_x(s_k)$  is advantageous to reduce the kick angle. Also a high value of  $\beta_x(s)$  helps in reducing the relative contribution to the kick angle due to septum thickness.

Thus, with  $\Delta \psi = \pi/2$ , we get ,

$$\theta_k = x_{close}(s) / \sqrt{\beta_x(s_k)\beta_x(s)}$$
  
and  $x' = -\alpha_x x_{close}(s) / \beta_x$ 



### Injection and Extraction (cont.) (a variation)

#### Box-Car stacking:

This is a variation on the fast injection or extraction scheme. This method is adopted quite often to fill a larger synchrotron (B) using a smaller synchrotron(A).

In this case the beam from the smaller synchrotron is transferred to the larger synchrotron in the form of batches (box-car) until the latter is filled.

The following conditions need to be met for an efficient Box-car stacking:

1. The beam is bunched in both machines and rf buckets are matched between the synchrotrons.

2. The kicker rise and fall time must be smaller than the bunch spacing or spacing between the "box-cars" in both machines.

Depending upon the length of kicker flat region, one can extract part or entire beam from the accelerator.

At Fermilab we adopt this method to

1. Fill MI using Booster (up to six batches)

2.Fill Tevatron using Main Injector (36 times for p and 9 times for antiprotons)

3. Fill Recycler using Accumulator

4. To extract protons for pbar production and for NuMI experiment (use two different extraction systems)

Efficiency of this technique is ~100%





### Injection and Extraction (cont.)

Orbit Bump (an application of dipole error):

To get better matching during extraction or injection the orbit of the beam can be bumped by using a set of trim dipole dipoles. For example,

- a. Three dipoles for "3-bump"
- b. Four dipoles for "4-bump"

These bumps are designed such that the closed orbit outside the bump remains unchanged.





### Injection and Extraction (cont.)

Orbit in Reality

In reality we will have focusing and defocusing quads in between dipole trims which form orbit bumps.

<u>3-Bump:</u>







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### **Multi-turn Injection**

This involves use of,

- a. Septum
- b. A programmed orbit bump in the vicinity of the septum

In case of protons, the orbit bump is reduced with time so that the early beam occupies the central region of the horizontal acceptance and the later beam occupies periphery of the acceptance. By the end of the injection the bump is reduced to zero.

This scheme evidently gives rise to emittance dilution. Generally,

the resulting emittance is

$$\varepsilon_{result} > 1.5n\varepsilon_i$$
  $n =$  number of turns

Here the issues are

1. Space charge in-coherent tune shift

2.Non-linear forces

#### <u>Betatron Phase-space-painting:</u>

During the multi-turn injection, if the betatron tunes ( $v_x$  and  $v_y$ ) and orbit bump are properly adjusted then the particle distribution in the transverse phase-space can be optimized. This is called transverse phase-space painting.

#### Longitudinal Phase-space-painting:

If the injection is done by slowly varying the injection RF phase during bucket to bucket transfer then the beam will be painted longitudinally.





### Charge Exchange Injection

Concept of H-charge exchange is invented at the Budker institute, Russia, (Budker and Dinov, Novosibirsk). Principle of charge exchange is adopted in this technique. This needs a 3-bumps or 4-bumps at the time of injection.



The steps involved in this scheme are

1. The closed orbit of the circulating beam is bumped onto the injection orbit of H beam.

2. The injected  $H^-$  beam and the circulating proton beam is made to go through a thin carbon foil (thickness of about 10-400 ug/cm\*\*2). In this process the electrons will be stripped off the  $H^-$  ions.

3. Since the constraints imposed by Liouville's theorem on conventional multi-turn injection does not apply here (because the charge states of the injected beam and circulating beam are different), one can inject several turns (2-40 turns). 4. Orbit bump is removed after the injection.

The injected beam can also be painted in transverse phase space by changing the closed-orbit bump.

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### Additional Injection/Extraction Schemes

Resonant Extraction:

Beam particles can be peeled off by using

1.3<sup>rd</sup>-order or

2.half-integer resonances

in a controlled fashion. The large amplitude particles moving along the separatirx are intercepted by **a thin septum wire** and are kicked off to another septum and transported to experimental area.

#### <u>Combined Cooling and stacking: (S. van der Meer, CERN)</u>

In this case each antiproton pulse (containing about ~1E7 particles) is

1. First subjected to fast longitudinal cooling

2.Next these antiprotons are deposited by an **rf system** at the high momentum edge of a stacked beam

3. This beam undergoes stochastic cooling and makes room for next similar transfer In this manner about 40,000 beam pulses are injected in about 24 hrs.

#### Longitudinal Phase-space Coating: (C. Bhat, Fermilab)

In this case each antiproton pulse (containing about 3E11 particles) is 1.injected using a fast injection scheme into a barrier bucket in a synchrotron. 2.Then these antiprotons are coated in longitudinal phase space in the form of ribbon over already existing beam captured in another barrier bucket. 3.This can be repeated as many times as the momentum acceptance of the machine allows. (At Fermilab we demonstrated up to 5-coats for antiproton transfer from Accumulator Ring to the Recycler).



# Lecture 4 (part-2)

# Practical Issues: Accelerator Commissioning

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### Commissioning of an Accelerator

Now let us address issues involved in commissioning of beamlines and accelerators. In an ideal world, if every thing is set according to theoretical calculations the machine just works as we have designed. In reality, there can be a number of issues like,

- 1. Magnets not built exactly to our specifications
- 2. Misalignment errors in the installation of magnets or issues with diagnostics.

Commissioning of any accelerator has never been an easy job.

Assumptions:

- 1. Good diagnostics. This is an essential constituent of any accelerator or beamline.
- 2. The beamline/accelerator vacuum is good enough for the type of operation. For example,
  - a. For transfer lines vacuum ~ 10<sup>-7</sup> torr
  - b. For a low intensity rapid cycling accelerators a vacuum of  $10^{\text{-7}}$  to  $10^{\text{-8}}$  torr may be good.
  - c. For higher intensity we need better vacuum
  - d. For beam storage rings or collider vacuum > 10<sup>-9</sup> torr
  - 3. Beam can be steerable remotely
- 4. The accelerator is set to theoretically best tunes and chromaticities.



### Illustrations with Examples

The examples that I am going to give are specific to that at Fermilab. Commissioning of 1.MI8 Beamline  $\leftarrow$  Beamline between the Booster and the Main Injector 2.Main Injector  $\leftarrow$  Accelerator 3.Recycler  $\leftarrow$  Storage Ring

But, the general philosophy behind the commissioning other facilities, hadron or lepton system, is the same. The specific details will change.





### Accelerator Commissioning





### Prepare to Establish Beam: Initial Settings

#### Setting the Momentum:

MI8 beamline is a permanent magnet beamline with its lattice designed to accept 8 GeV protons . The admittance of the beamline is 40  $\pi$ -mm-mr and momentum acceptance of about 0.4% . These are fixed by design.

➡ (See Figure on next page)

To set the initial momentum, one adjusts the bend field of the machine, so that

 $p[GeV] = 0.2997 \times B\rho [Tm] = 8.889 \text{ GeV/c}$  (Table on page 18)

in the case of the Main Injector.

We assume that the RF frequency,

 $f_{rf} = h \times f_{rev} = h \times \frac{2\pi R}{\beta c}$  R is the Radius and  $\beta c$  = beam velocity = 52811400 Hz and R = 528.670 meter

is stable and the radius of the machine is fixed. If there are any drifts in voltage, it may be mostly due to power supplies. Sometimes the sources of the problems may be somewhere else. For example, in the case of new constructions the orbit drift can arise due to settling of the ground or ground motion. These issues need additional understanding/investigation.

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### Theoretical Lattice from MAD calculations





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### Main Injector and 8 GeV beamline Magnet counts

WBS LEVEL 4	=	Ring	8GeV	Spare	ISA (sextupoles)
IDA dipole 240"	N	108	-	5	MR trim quads
IDB dipole 240"	N	108	-	5	MR skew quads
IDC dipole 160"	Ν	64	-	4	MR skew sext
IDD dipole 160"	N	64	-	4	MR trim sext
PDD (perm dipl)	N	-	45		MR octupoles
PVD(vert dip)	N	-	4		CR quad - skew
EPB 5-1.5-120	R	-	4	1	
					HDC MR horiz tr
IQC (100.13" MI)	R	/ 32	\ -	3	HDD MR horiz tr
IQD (116.26" MI)	R	48		4	IDH MI horiz trin
IQB (84" MR) ring	R	122	-	6	VDC MR vert tri
IQE (84" MR) ring	R	4	-	2	HDR MR vert tri
IQF (84" MR) ring	R	1	-	1	IDV MI vert trim
SQA(17" P-Bar)	R	-	9	2	Lambertson 8 (
SQC(26" P-Bar)	R	-	5	2	Lambertson, 6 C
SQF (48" P-Bar)	R	-	2	1	C-Magnet FMI
PGD(gradient)	Ν	-	65		Iambertson, RR
IQG, rolled	R	1	-	1	
PQP (Perm quad)	N	-	9		

ISA (sextupoles)	N	(108	) -	6
MR trim quads	R	16	-	3
MR skew quads	R	16	-	3
MR skew sext	R	0	-	0
MR trim sext	R	0	-	3
MRoctupoles	R	66	-	5
CR quad - skew	R	4	-	1
HDC MR horiz trim	R	-	26	5
HDD MR horiz trim	R		-	3
IDH MI horiz trim	N	/ 104	-	15
VDC MR vert trim	R	-	18	9
HDR MR vert trim	R	-	7	2
IDV MI vert trim	N	104	-	6
Lambertson, 8 GeV	R	-	1	1
Lambertson, FMI	N	-	-	4
C-Magnet, FMI	N	-	-	4
Lambertson, RR	N	-	-	2
	Totals	970	195	183



### Initial settings (cont.)

#### Relevant 8 GeV Booster Parameters:

1.Beam KE= 8 GeV 2.Transverse Emittance 10-20  $\pi$ -mm-mr 3. Harmonic number= 84 4.RF frequency= 52811400 Hz 5.Vrf(extraction) = 375kV 6.RF bucket half height = 33.4 MeV 7.Beam Intensity ~ 0.5E10- 6E10 p/bunch

#### Relevant MI RF Parameters to be set to:

1.Beam KE= 8 GeV 2.Transverse Emittance 10-20  $\pi$ -mm-mr 3. Harmonic number= 588 4.RF frequency= 52811400 Hz 5.Vrf(Injection) = 1.05MV 6.RF bucket half height = 33.4 MeV 7.Beam Intensity ~ 0.5E10- 6E10 p/bunch

Beam diagnostics in the Beamline:Multi-wires:15 Multi-wire scanner systems are in the beamline.1.8 in Vertical planes2.7 in Horizontal planes4 Multi-wire scanner systems in the MI+ one in the Abortline.1.2 in Vertical planes2.2 in Horizontal planesInsert all of these before injecting the beamBPM:Beam Current Transformers:SeveralSeveral toroids

All of them to be enabled.

Inject the beam. From the safety point of view start with minimum beam as needed.

# MI8 Loss Monitor Data





Yes! There is some beam got transported through the tunnel but, no BPMs lit. Beam energy may be wrong?, Some upstream magnetic field settings may be wrong? Many questions?

#### MI8 Beamline Multi-wire data (Earliest attempt) (September 26, 1998)





## MI8 Beamline Multi-wire data (cont.)

(September 26, 1998)



Booster to MI injection region has a "dogleg" in its lattice - beam is kicked vertically and bent down by about 8 feet before the permanent magnet region starts. There are only a few electromagnet devices which can be adjusted.

After tweaking some injection devices, the beam reached the end of the beamline. (about 760m long)

For a group of experts this took about 8 hours to reach this stage. These people were responsible for designing this beamline



#### Current Transformers Data (September 26, 1998)





#### MI8 beamline BPM Data (September 26, 1998)





#### 1<sup>st</sup> Beam in the MI, Current Transformers Data (September 26, 1998)





### MI8 Beamline & MI Multi-wire data (cont.)





### Kicker profiles



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#### MI BPM Data (October 3, 1998)





#### MI BPM Data (October 3, 1998)



Experts figured out that there is about 1.9 deg roll angle in the injection Lambertson magnet and Booster injection energy was off by about 25 MeV. We can proceed only after fixing these problems.

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#### 1<sup>st</sup> Beam in the MI, Current Transformers Data (October 10, 1998)



#### 1<sup>st</sup> Circulating Beam in the Main Injector BPM Data (October 3, 1998)



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#### More stable in the MI, Current Transformers Data (October 11, 1998)







#### MI8 Beamline & MI Multi-wire data (cont.) (October 18, 1998)



Good transmission and beam profiles in all of these MWs!





### 1<sup>st</sup> Tune Measurement and Transverse Phase-space plot using TBT

<u>Tune measurements using Turn-by-turn (TBT)</u>: An FFT of BPM data taken after exciting oscillations shows a peak at the machine's tune value.



Close to 8<sup>th</sup> order resonance. Beam survives but not good!!

### H and V-Tune Measurement and Transverse Phase-space plot using TBT (cont)



We ping the beam in the horizontal plane using a kicker soon after beam injection

> Design  $v_x = 0.425$  $v_y = 0.415$





Measured  $v_x=0.426$  This is away from any resonances. Still not a good region!  $v_y=0.405$  This is a separate measurement after pinging the beam vertical plane



### Tune point on the Tune Diagram



for better beam

transmission



### Tune Scan for Recycler



From Cons Gattuso

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### Measuring the Integer part of the Tune

Measuring the integer part of the tune involves a.Measuring the difference orbit with and without a dipole kick on the orbit b.Count the number of betatron oscillations





### Smoothing the Orbit

<u>Goal:</u> In a high energy synchrotron, one generally will have several 2- and 3-bumps for 1.beam injection

2.extraction and

3.for special beam gymnastics

Nonetheless, the machine orbit should be "undisturbed" outside these bumps. If not, these locations become the main sources of transverse emittance dilution and beam losses.

Need to establish new closed orbit and open the dynamic aperture.

This step is an iterative procedure and needs

1.Reliable BPM system to measure the orbit accurately

2.A number of dipole correctors



### Smoothing the Orbit (cont.)



#### (1<sup>st</sup> turn - 2<sup>nd</sup> turn) before smoothing







Vertically it improved significantly during this smoothing.

#### Stable Beam in the MI with good beamlife time, (November 8, 1998)





### Injection Closure or beamline Tuner (BLT)

<u>Goal:</u> Match the injection orbit to that of the closed orbit

Advantages: Eliminate transverse emittance growths associated with the injection

This technique has two steps: 1.Calibrate the BLT 2.Implementation of BLT Requirements: 1.Two correctors C1 & C2, in the injection beamline which are separated by a phase advance of  $\pi/2$ 2.A BPM in the ring sensitive to beam intensity of interest

#### Calibration: Measure

 $S1 = \frac{\text{Beam oscillation Amplitude from TBT}}{\text{Corrector Strength (Amp)}}$ 

for C1 keeping C2 constant. Similarly S2 for C2.

<u>Implementation</u>: Inject the beam and measure the amplitude & the phase of the beam at BPM by fitting TBT data. Using S1 and S2 one can determine exact amount of corrector strengths needed to achieve

```
\DeltaAmplitude = 0
\DeltaPhase = 0 at the injection point
```





#### Injection Closure Accumulator pbars → Main Injector (Calibration of BLT)

#### Calibration for Horizontal Injection Closure:



Issues in these calibrations: These two dipole correctors were not exactly 90deg apart? There are some hysteresis effects.

Similar calibration is carried out for the Vertical plane

### Example on Injection Closure (cont.) Accumulator pbars → Main Injector





# Recycler Beamline Tuner



#### An Example on Injection phase and Energy Tuning (Longitudinal) Booster protons→ Main Injector $\frac{V\cos(\phi_s)}{h\eta}$ Matching RF : Voltage at 8 GeV $V\cos(\phi_s)$ h V MV η = hη 180 84 0.0223 0.375 Booster



### Measurements of Admittances

There are two types of admittances to be measured and optimized:

- 1. Transverse admittance
- 1. Transverse admittance 2. Longitudinal admittance  $\leftarrow \left[\frac{\Delta p}{p}\right]_{\mu}$

#### Transverse admittance

Different methods are used for accelerators and beam storage rings. An example of admittance measurement in the Recycler is shown here.

- 1. Inject the beam,
- 2. Heat the beam by pinging till it fills up the entire aperture
- 3. Move a scraper till it touches the beam as observed by a loss monitor
- 4. Move the scraper till all the beam disappears.

### Then admittance is given by

$$A = \frac{6\pi\beta\gamma\sigma^2}{\beta_{lattice}}$$
 For the non - dispersion region

Similarly for the other plane

#### Long. Admittance :

Inject the beam into an RF bucket and change the rf freq. up and down till beam touches the aperture point.



 $\frac{\Delta p}{p} = -\frac{1}{\eta} \frac{\Delta f}{f}$ 

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Opening the Aperture (Aperture Scan)

It is highly essential to optimize the aperture for the best beam transmission.

FTP V5.12 Console SA 25-0CT-98 00:57 Pri=2 This is done by 1 Sun 2 co\_ 0.00.0010 \_0/02\_0.0 monitoring the beam loss ö n as the beam is moved by Loss monitor data ō ö varying the magnet dipole 9 corrector strength at 1.5 ີບ 0 that location. Available 0 I:43BLMA VOLT 0 ŝ Aperture 80) 0 in H-plane 1 â 0 Ω. 0 n The best <15 Hz > This procedure should be Ū setting repeated at every point in ξŪ .5 the Ring/transfer lines. 0 n íŪ. n ΠO 0.00 001 ø  $\overline{04}$ 0 0 . 5 < 15 I:H400 D∕A Unit engineering units

Similarly for the vertical plane



### **Beam Acceleration**



Setup acceleration Ramps: a.Magnet ramp for dipoles, guads, sextupoles, all correctors V<sub>rf</sub>=1-3.4 MVb.Set RF voltage curve c.Set proper accel. phase d.Radial feed-back (this is to keep the rf frequency synchronous with the dipole e. Transition phase jump f.Proper orbit, tunes,

chromaticities.

In an ideal case, beam will be accelerated as desired with above settings. But, ??



### Beam Acceleration (cont.)



# Tweaking the Radial Feed-back & Accel. Phase Angle

Whenever there is a large frequency swing from injection energy to the top energy, one uses a radial feedback to keep the beam in the center of the machine during acceleration.



### Example of Radial and Phase detectors in the MI Ring



MI612 2.5MHz Rpos Det.

MI603 Longitudinal Kicker 2.5MHz Phase Det.





### Beam Acceleration (cont.)

It is highly essential to keep

- 1. Beam in proper tune space
- 2. Chromaticity space and chromaticity jump across the transition

throughout the beam acceleration so that machine will not cross any dangerous resonances.



Similarly for the vertical plane



### **Transition** Crossing

Transition crossing is one of the major issues for hadron synchrotrons. For example, the synchrotron frequency at transition is

$$[f_s]_{Transition} = \sqrt{\frac{eV_0 h \eta \omega_s \cos \phi_s}{2\pi p_s R_s}} \to 0 \quad \& \quad \frac{\Delta p}{p} \to \infty$$

This implies the phase focusing disappears and particles get **FROZEN**. Further, the particles change their direction of motion in  $(\Delta E, \phi)$ -phase space as it crosses the transition.

.. It is highly essential to
1.Change the rf phase from rising side of the rf wave to falling side of the wave, (phase jump)
2.Set proper time for transition phase jump.
3.Match the rf voltage before & after transition crossing
4.Keep the radial position of the beam un-disturbed,

Consequence of not doing these are a)longitudinal emittance growth b)may be beam loss.

In some hadron accelerators special transition crossing schemes are used.



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### Experiments on Transition Crossing (cont.)

(Adjusting the crossing time)







### Beam in MI on 8-120 GeV cycle



Have accelerated >5E12p



### Kicker Profiles for Multi-batch Injection





### **Beam Measurements**

#### Beam Properties of Interest:

- 1. Beam Intensity 🗸
  - $\checkmark$
- 2. Global Quantities
- a) Tunes
- b) Chromaticity
- 3. Lattice Measurements
- a) Orbits: Flash, Display, Profile

 $\sqrt{}$ 

- b) Dispersion measurements
- 4. Emittances:
- a) Transverse Emittance: H and V
- b) Longitudinal Emittance

And so on





### **Chromaticity Measurements**

To the 1<sup>st</sup> order, the chromaticity  $\xi$  is given by,  $\Delta v = \xi \frac{\Delta p}{\Delta r}$ p

Further, we have the following relation,  $\frac{\Delta p}{p} = -\frac{1}{\eta} \frac{\Delta f}{f}$ 

Thus, by measuring tune as a function of 
$$\Delta p/p$$
 , one can measure the chromaticity.

In the case of Main Injector, 1. the reference value for the radialfeed-back loop is nominally "O" 2.changing it by a few mm leads to change in rf frequency 3.Since.

$$x = x_{co} + D(s) \frac{\Delta p}{p}$$
 or  $\frac{\Delta p}{p} = \frac{x - x_{co}}{D(s)}$ 

Comparison between new orbit and the closed orbit and knowing D(s), one can measure  $\Delta p/p$ 

By changing the radial position offsets, one can set different values for  $\Delta p/p$ . Thus, chromaticity can be measured.

The tune is measured by TBT data for each set of  $\Lambda R$ .





### **Dispersion Measurements**

To the  $1^{s^{\dagger}}$  order the dispersion function D(s) is given by,

$$\Delta x = D_x(s)\frac{\Delta p}{p} = -D_x(s)\left[\eta\frac{\Delta f}{f}\right]$$





### Beam Emittance Measurements

#### <u> Transverse Emittance:</u>

Transverse beam profile monitors are used to measure the beam size . For example, if  $\sigma_{\rm x}$  is the measured beam size in non-dispersive region, then,

$$\sigma = \sqrt{\frac{\varepsilon_x \beta_x}{6\pi\beta\gamma}}$$

is used to measure the transverse emittance  $\mathcal{E}_x$  (normalized)

#### Longitudinal Emittance

This is the beam area in  $(\Delta E, \phi)$  phase space. For the beam in sinusoidal stationary bucket, if  $\Delta$  is the bunch length measured using "wall current monitor", then the longituidnal emittance is obtained by,

$$LE = \sqrt{32} \frac{V_0 R_s^2 E_s}{2\pi h^3 c^2 |\eta|} \int_0^{\frac{1}{2}} \sqrt{\cos(x) - \cos\left[\frac{\Delta}{2}\right]} dx \text{ and}$$

"Half Beam Height,  $\Delta E$ " = Bucket height × sin  $\left| \frac{\Delta}{4} \right|$ 

Vo=0.05MV, Rs= 528m, Es= 27 GeV, h=28,  $\eta$ =0.001,  $\Delta$ =46 nsec give LE= 1.95 eVs and  $\Delta p/p$ =0.1%

Vo=0.55MV, Rs= 528m, Es= 150 GeV, h=588,  $\eta$ =0.0021,  $\Delta$ =9 nsec give ~ LE= 1.95 eVs and  $\Delta p/p$ =0.1%



### Beam Emittance and Tune Measurements (using Schottky Signals)

Use of Schottky signals in measurements of beam properties is one of the most wonderful technique for storage rings. These signals can be used to measure

- Longitudinal emittance
   Beam intensity
- 4. Tune of the machine,
- Transverse emittances 5. Chromaticity

Longitudinal Schottky data





<u>Longitudinal Emittance, Energy spread & Beam Intensity:</u> Measure the longitudinal Schottky spectrum using a longitudinal Schottky detector. Then,

Total Schottky Power 🛇 Beam intensity

RMS width OC RMS Momentum spread

RMS LE =  $\pi(\sigma \times \text{RMS}$  Bunch Length from wall current monitor)

#### <u> Transverse Emittance:</u>

Measure the transverse Schottky spectrum using a transverse Schottky detector. Then,

Total Schottky Power of the side band

C Transverse emittance

#### <u>Transverse Tune:</u>

The distance of the sideband from the center peak is a measure of fractional tune of the machine.

Chromaticity:

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The width of the sideband is measure of the tune spread.

*Chromaticity* = 
$$\xi = \Delta v / \frac{\Delta p}{p}$$





### Accumulator Horizontal Schottky Spectrum

