

Resonant and non-resonant magnetic x-ray diffraction

Dinesh Kumar Shukla

UGC-DAE Consortium for Scientific Research, Indore

dkshukla@csr.res.in

www.csr.res.in

Contributors

Scientific staff at P09, PETRA III, DESY, Hamburg, Germany

Joerg Stempfer, M. v. Zimmermann
Sonia Francoual,
Arvid Skaugen,
Helen Walker

Technical staff at P09 at DESY, Hamburg, Germany

David Reuther
Rainer Doiring
Kathrin Pflaum
Rudiger Nowak



Department of Physics, Indian Institute of Science, Bangalore, India

Dona Cherian, Suja Elizabeth

L.V. Kirensky Institute of Physics Siberian Branch of Russian Academy of Sciences

Leonard N. Bezmaternykh, Irina A. Gudim, Vladislav L. Temerov



Few basic information related to synchrotron radiation/X-rays

What do we get from synchrotron sources ?

From synchrotron sources we receive **very high intensity polarized x-rays**.

X-rays wavelength is 0.01 nm to 10 nm. (120 keV to 120 eV) [$E(\text{keV})=12.39/\lambda(\text{\AA})$]

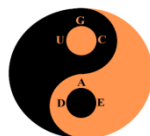
Upto few keV (2 to 3) it is called soft x-rays and above it is called hard x-rays.

How is the synchrotron radiation generated ?

Synchrotron radiation is generated by rotating a charged particle in a circular orbit at a relativistic speed. Radiation is generated in the tangential directions of the circle.

Why do we need synchrotron X-rays

To study the structure of matter through different fundamental processes like scattering, diffraction, reflectivity, absorption, fluorescence.



Outline

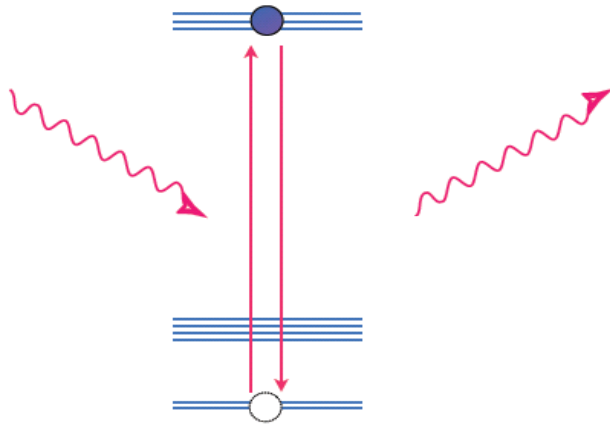
- **Concept of resonant X-ray diffraction**
- **Resonant and non-resonant magnetic X-ray diffraction**
- **Experimental requirements**
- **Some examples**
 - **Multiferroic “rare earth iron borate”, $\text{HoFe}_3(\text{BO}_3)_4$**
 - **Chiral properties of hematite ($\alpha\text{-Fe}_2\text{O}_3$)**
 - **Coexistence of Superconductivity and ferromagnetism in P-doped EuFe_2As_2 .**



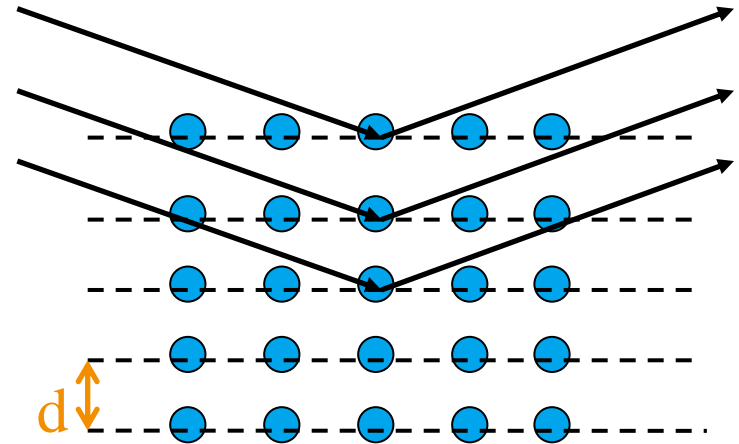
Resonant x-ray diffraction

This technique combines the spectroscopy and diffraction phenomenon

Spectroscopy

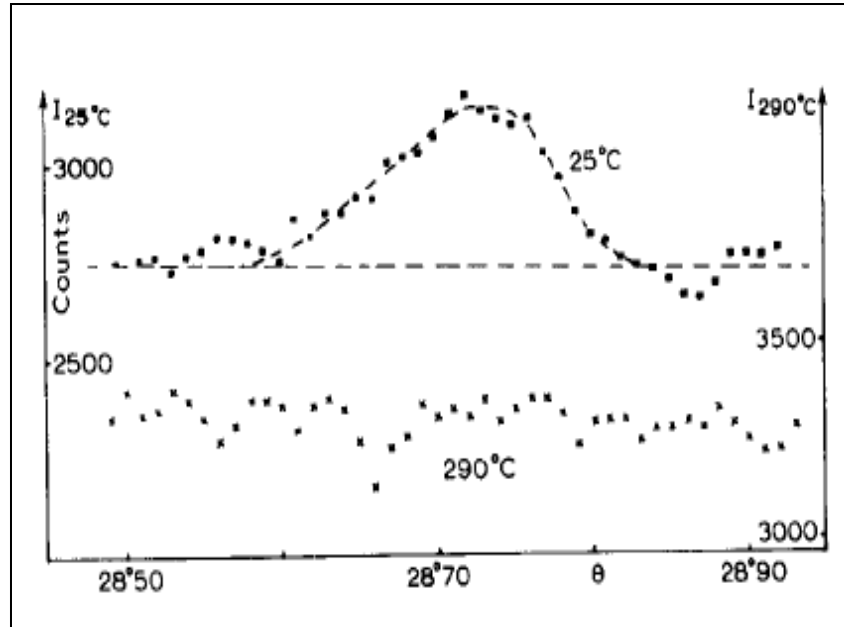


Diffraction $\lambda = 2 d \sin \theta$



Diffraction at absorption edges

Observation of first x-ray magnetic peak in NiO



$(3/2\ 3/2\ 3/2)$ peak, 3 days counting time for each curve

Bergevin, F. de & Brunel, M. (1972) Phys. Lett. A 39, 141.

Observation of first magnetic superlattice peaks by x-ray diffraction in NiO



Why magnetic x-ray diffraction?

- Can be used for investigations of **submillimeter-sized** single crystals.
- Many of the technologically important RE compounds contain **neutron opaque elements**.
- **Superior reciprocal space (Q) resolution** allows more detailed study ... reinvestigation of “solved” structures.
- Resonant magnetic scattering occurs at well-defined **energies specific to elements of interest** -- probe local magnetism.
- **Orbital moment** determination
- Studies of **magnetic surfaces and interfaces**.



Magnetic x-ray diffraction

Elastic scattering amplitude for scattering from magnetic ion:

$$f = f_0 + f' + if'' + f_{mag}$$

At resonance:

$$f \approx (\epsilon' \cdot \epsilon) F^{(0)} - i(\epsilon' \times \epsilon) \cdot \mu F^{(1)} + (\epsilon' \cdot \mu)(\epsilon \cdot \mu) F^{(2)}$$



Resonant and non-resonant magnetic X-ray diffraction scheme with polarization analysis

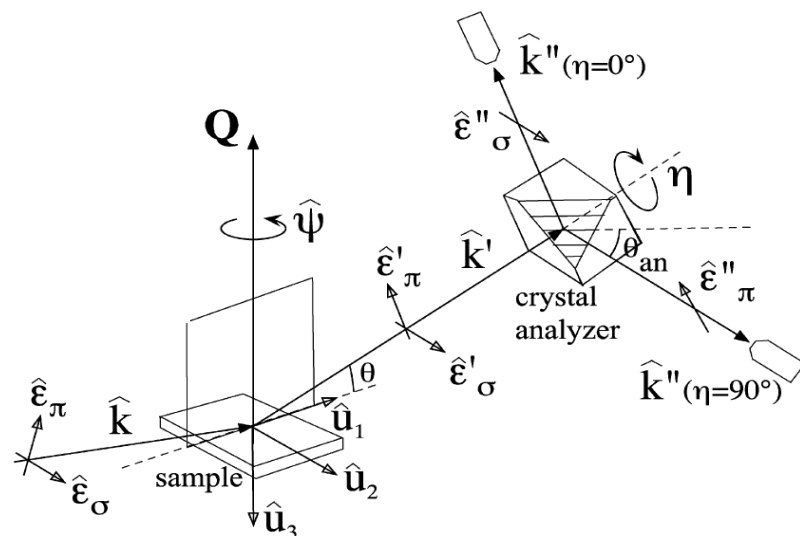
Resonant magnetic scattering amplitude (electric dipole transitions) [Hill & McMorro]

$$f_{E1}^{res-mag} = \begin{pmatrix} f^{\sigma\sigma'} & f^{\sigma\pi'} \\ f^{\pi\sigma'} & f^{\pi\pi'} \end{pmatrix}$$

$$= F^0 - iF^1 \begin{pmatrix} 0 & m_1 \cos \theta + m_3 \sin \theta \\ m_3 \sin \theta - m_1 \cos \theta & -m_2 \sin 2\theta \end{pmatrix}$$

$$+ F^2 \begin{pmatrix} m_2^2 & m_2(m_1 \sin \theta - m_3 \cos \theta) \\ m_2(m_1 \sin \theta + m_3 \cos \theta) & -\cos^2 \theta(m_1^2 \tan \theta + m_3^2) \end{pmatrix}$$

Strong intensities due to resonance enhancement
 Element sensitivity at absorption edges
 Magnetic structure determination



Non-resonant magnetic scattering amplitude [Blume & Gibbs]

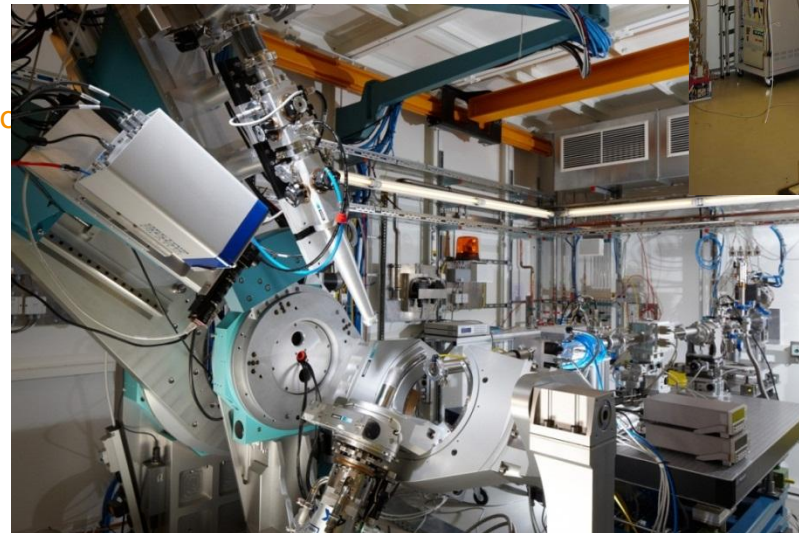
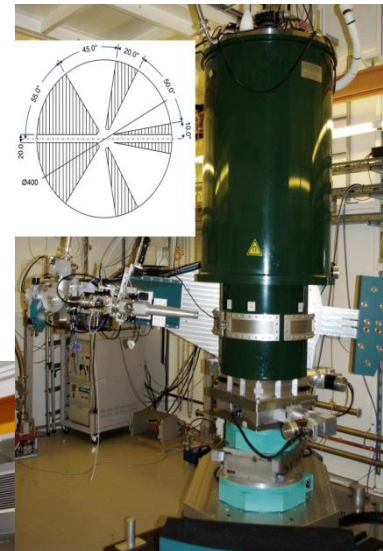
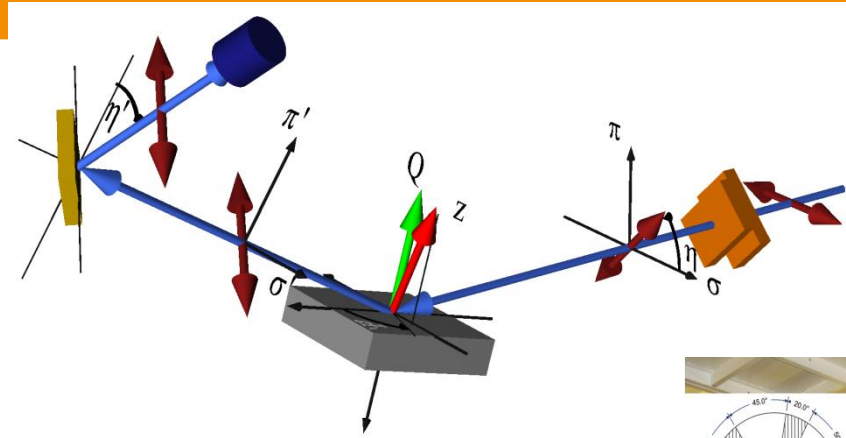
$$f^{mag} = -i \frac{\hbar\omega}{mc^2} \begin{pmatrix} f^{\sigma\sigma'} & f^{\sigma\pi'} \\ f^{\pi\sigma'} & f^{\pi\pi'} \end{pmatrix}$$

$$= -i \frac{\hbar\omega}{mc^2} \begin{pmatrix} S_2 \cos \theta & \sin \theta [\cos \theta (L_1 + S_1) + S_3 \sin \theta] \\ \sin \theta [-(L_1 + S_1) \cos \theta + S_3 \sin \theta] & \cos \theta [2L_2 \sin^2 \theta + S_2] \end{pmatrix}$$

Determination of L/S ratio
 Magnetic structure determination



Resonant Scattering and diffraction experiment, at beamline P09, PETRA III



- Energy variation:
 - Large energy range: 2.7 keV – 50 keV
- Small beam focus
 - Beam size routinely (mirror): $145 \times 40 \mu\text{m}^2$
 - with Compound Refractive Lenses: $\sim 50 \times 4 \mu\text{m}^2$
- Effective higher harmonic suppression
 - High harmonic suppression in full energy range 2.7 – 24 keV
- Variable x-ray polarization
 - Fully variable incident polarization in energy range 3.4 – 8 keV (2.7 – 13 keV)
 - Analysis of scattered polarization states
- Psi-diffractometer (EH1)
 - Open χ -circle \rightarrow large accessible angular range
 - Quasi-simultaneous use of area and point detectors
- Heavy Load Diffractometer (EH2)
 - Horizontal 6-circle diffractometer
 - 650 kg load maximum
- Special sample environments
 - Several low temperature cryostats
 - High magnetic fields: 14T magnet, He-3 insert
 - Temperature range $300 \text{ mK} < T < 800 \text{ K}$

Role of magnetic structure in multiferroicity:

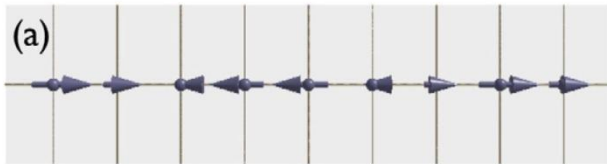
$\mathbf{P} = \mathbf{e}_3 \times \mathbf{Q}$;
 where $\mathbf{e}_3 = \mathbf{S}_i \times \mathbf{S}_j$; and \mathbf{Q} is the wave vector
 direction.

[M. Mostovoy, Phys. Rev. Lett. 2006, 96, 067601.]

[H. Katsura et al., Phys. Rev. Lett. 2005, 95, 057205.]

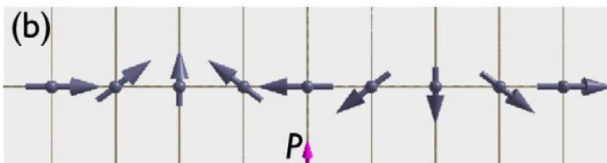
Example: TbMnO_3

$T_S < T < T_N = 42 \text{ K}$

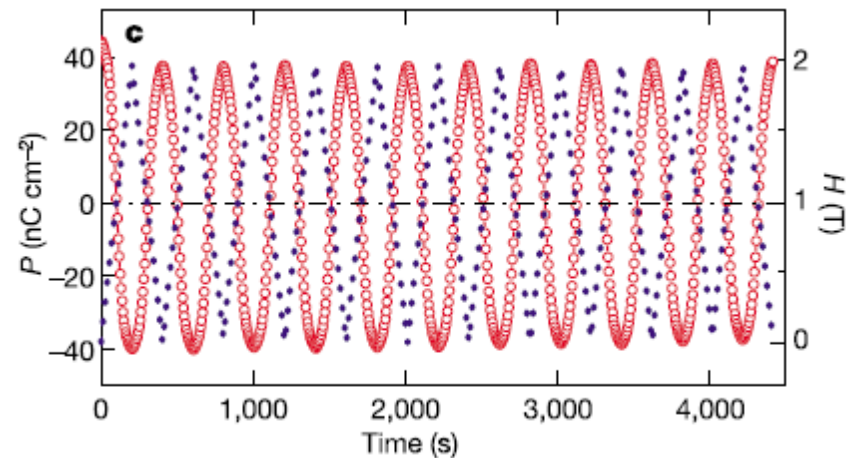


$P = 0$

$T < T_S = 28 \text{ K}$



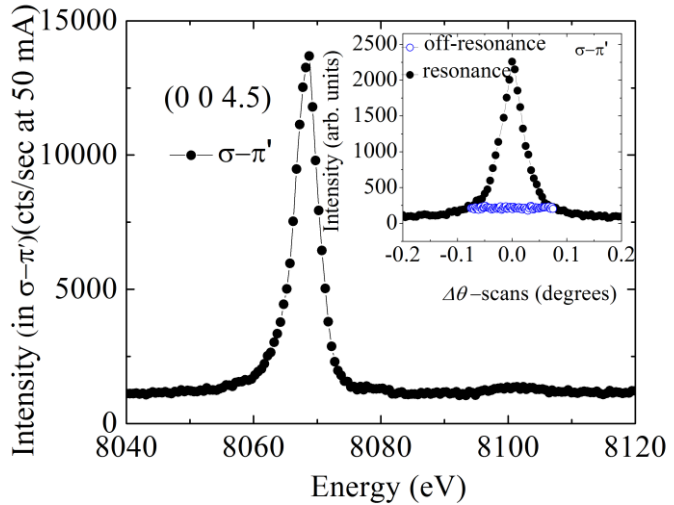
$P \neq 0, P \parallel C$



Polarization flipping by linearly varying magnetic fields from 0 to 2 T in TbMn_2O_5 .
 (Nature **429**, 392 (2004)).

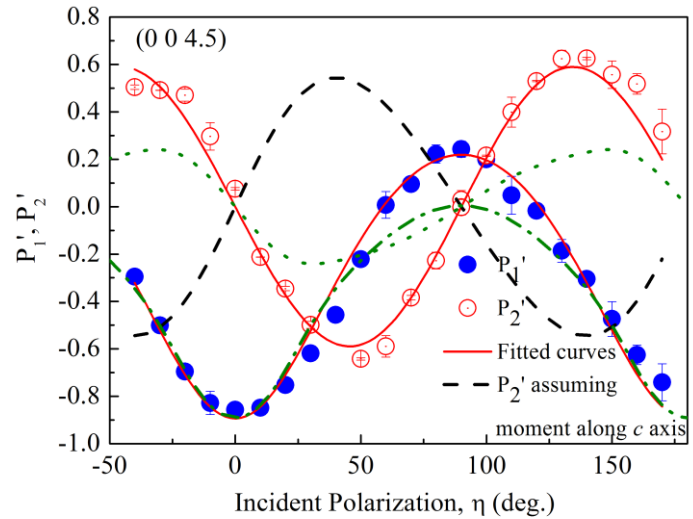
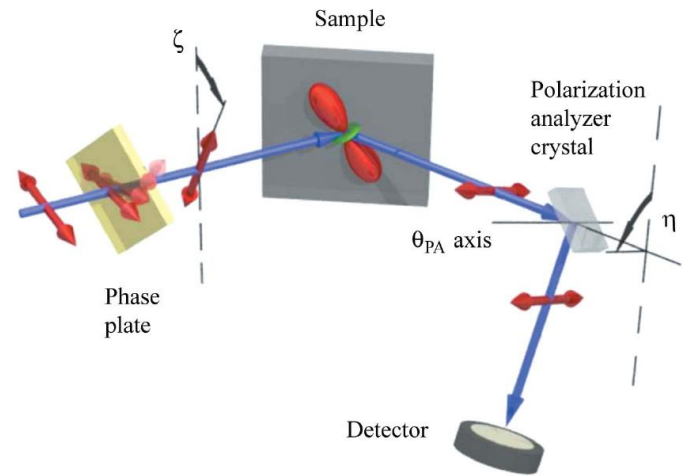


Determination of ab-plane spin spiral of Ho moments in $\text{HoFe}_3(\text{BO}_3)_4$ through Full polarization analysis at resonance at P09, PETRA III



Energy scan at Ho L_3 edge on $(0, 0, 9/2)$ at 6 K,

D. K. Shukla et al. *Phys. Rev. B* **86**, 224421 (2012).



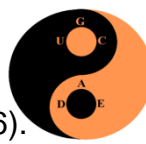
Fitting of Poincaré-Stokes parameter:

$$I(\eta, \eta') = \frac{P_0}{2} (1 + P_1'(\eta) \cos 2\eta' + P_2'(\eta) \sin 2\eta')$$

Full polarization analysis at Ho L_3 edge on $(0, 0, 9/2)$ at 6 K,

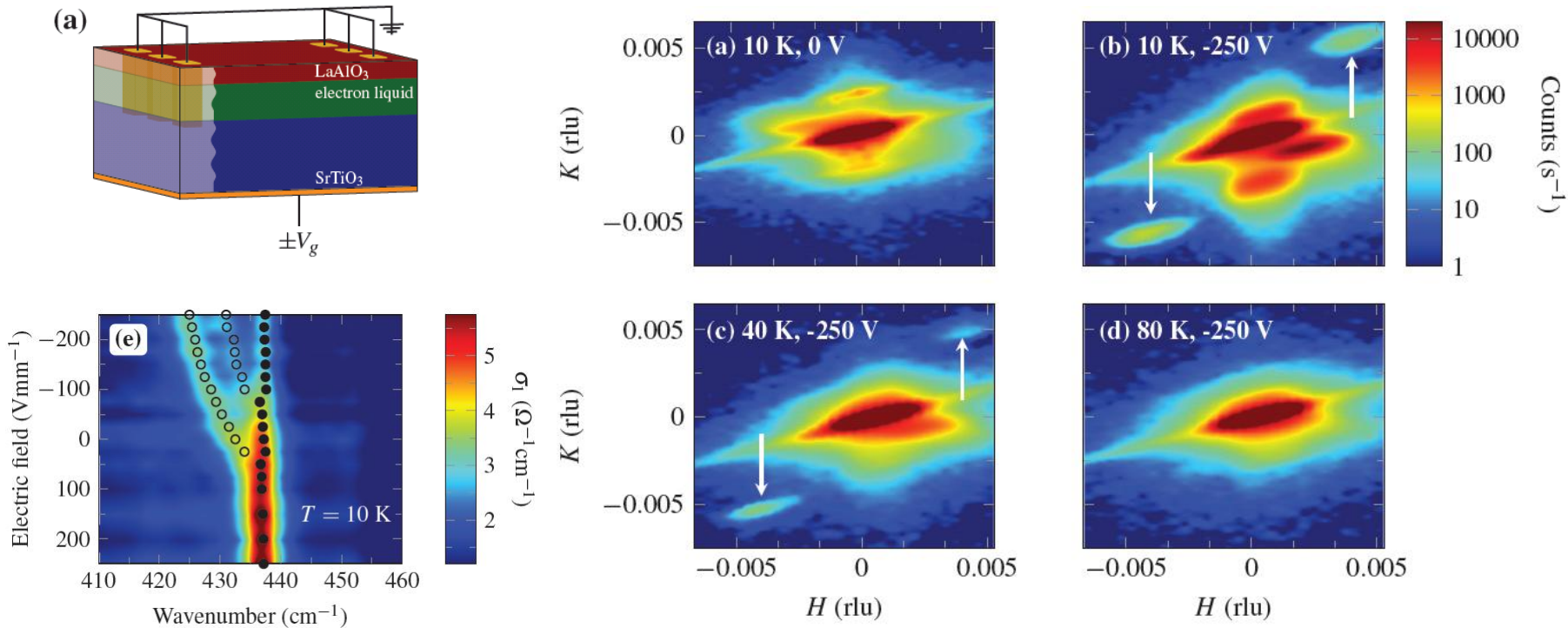
Ho moments are forming ab-plane spin spirals, making a screw-type magnetic structure.

C. Mazzoli et al., *PRB* **76**, 195118 (2007).
 M. Blume and D. Gibbs, *PRB* **37**, 1779 (1988).
 Hill and McMorro, *Acta Cryst.* **A52**, 236 (1996).

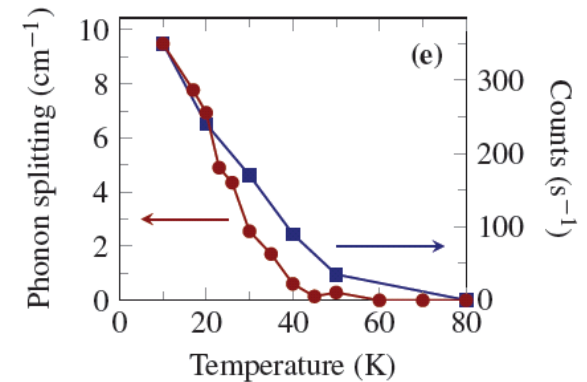


Electric field effect on the confined electrons at the LaAlO₃/SrTiO₃ interface

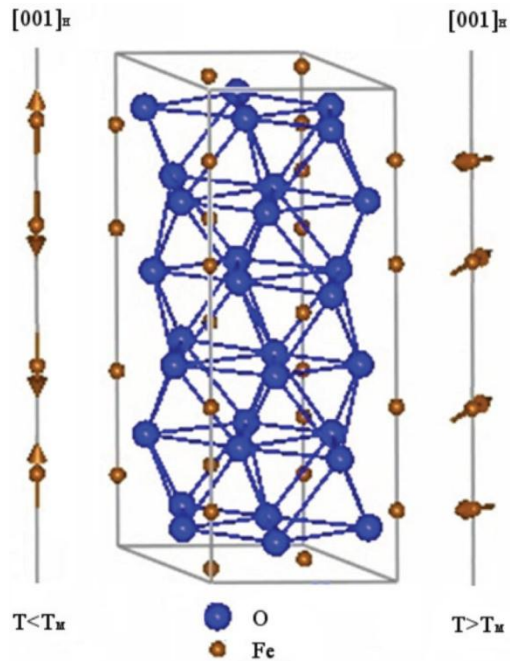
M. Roessle et al. *Phys. Rev. Lett.* **110**, 136805 (2013)



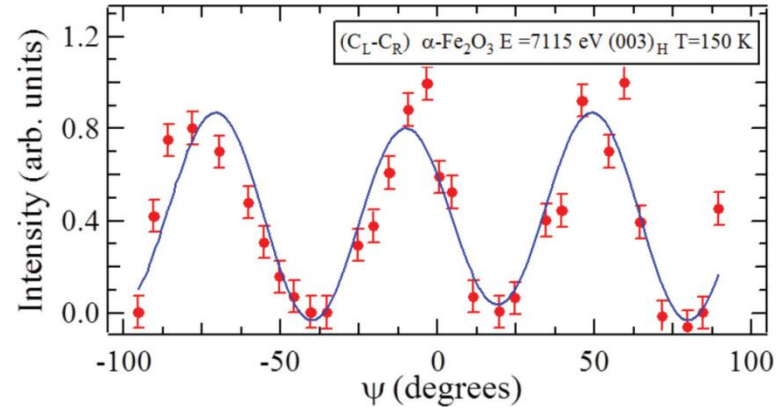
- field induced polar layer in SrTiO₃
- localization of electrons for negative gate voltage
- satellite peaks with 60 nm period develop parallel to the LAO/STO interface



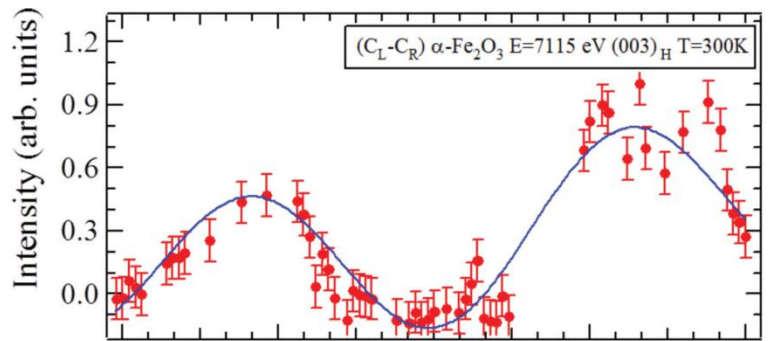
Chiral properties of $\alpha\text{-Fe}_2\text{O}_3$, investigated using circularly polarized X-rays



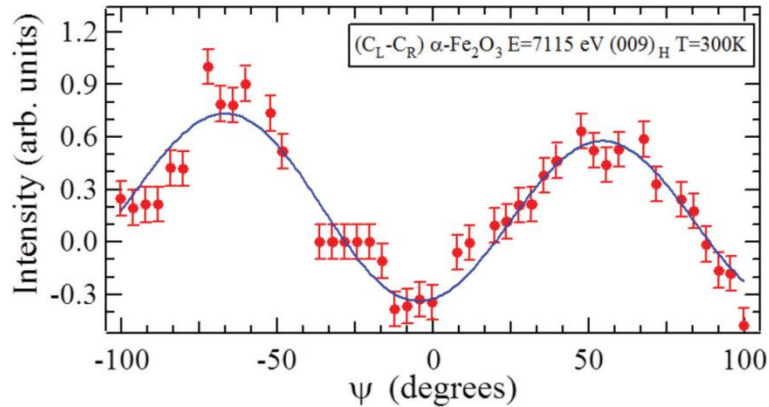
A. Rodriguez-Fernandez et al. **Phys. Rev. B** **88**, 094437 (2013)



Phase-I



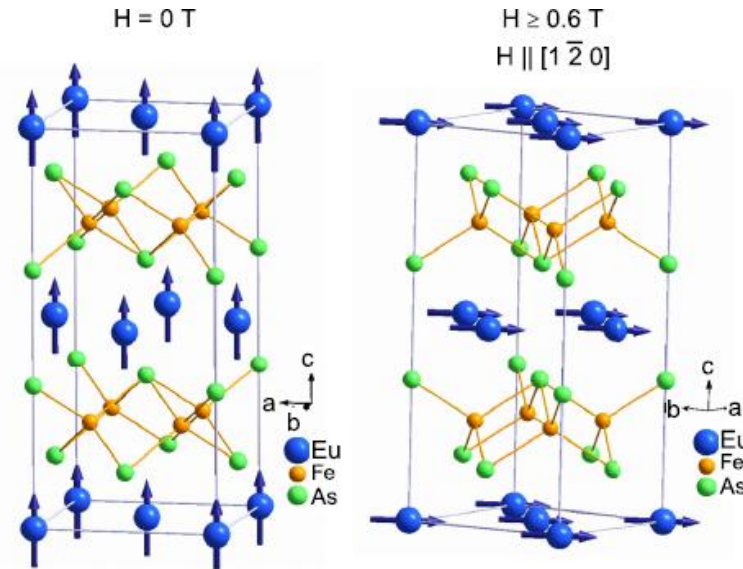
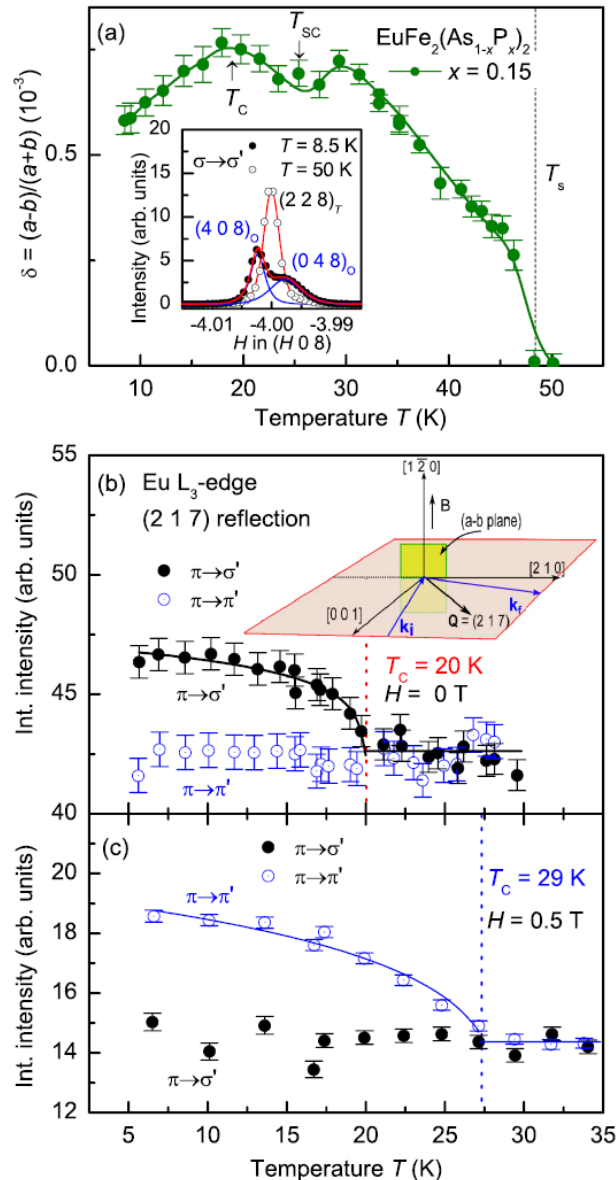
Phase-II



- circular polarized incident x-rays tuned near the iron K edge was used.
- Magnetoelectric multipoles, fully characterize the high-temperature canted phase.
- Orbital angular momentum accompanies the collinear motif, and it is absent in the canted motif.

Coexistence of Superconductivity and ferromagnetism in P-doped EuFe_2As_2

Nandi et. al., **Phys. Rev. B** 89, 014512 (2014)



➤ The long-range ferromagnetic order of the Eu^{2+} moments aligned primarily along the c axis coexists with the bulk superconductivity at zero field.

➤ Under an applied magnetic field, superconductivity still coexists with the ferromagnetic Eu^{2+} moments, which are polarized along the field direction.

➤ A spontaneous vortex state is proposed for the coexistence of superconductivity and ferromagnetism in $\text{EuFe}_2(\text{As}_{0.85}\text{P}_{0.15})_2$.

Thank you all for your kind attention.

